

# Exploring Black Holes, Second Edition

Edwin F. Taylor, John Archibald Wheeler, and Edmund Bertschinger

## For Instructors and Individual Readers

*Exploring Black Holes: Introduction to General Relativity* uses the properties of non-spinning and spinning black holes to introduce Albert Einstein's theory of curved spacetime and applies the resulting *general relativity* to the Universe around us. In this second edition -- labeled EBH2e -- coauthor Edmund Bertschinger joins Edwin F. Taylor to revise and expand the first edition by Edwin F. Taylor and John Archibald Wheeler published in 2000. What happened to the first edition? See the PS2 at the end of this document.

There is no published hard copy textbook of EBH2e. Instead, you may freely download the online version for personal and class use. Download one chapter or the entire book at the dropsite [exploringblackholes.com](http://exploringblackholes.com)

THE STRATEGY: In EBH2e we choose to make every measurement and observation in a *local* inertial frame, so we can analyse them using special relativity. This assumes that almost everywhere -- except possibly at the center of a black hole -- spacetime curves gently enough so that it is sufficiently flat over a small region to use special relativity.

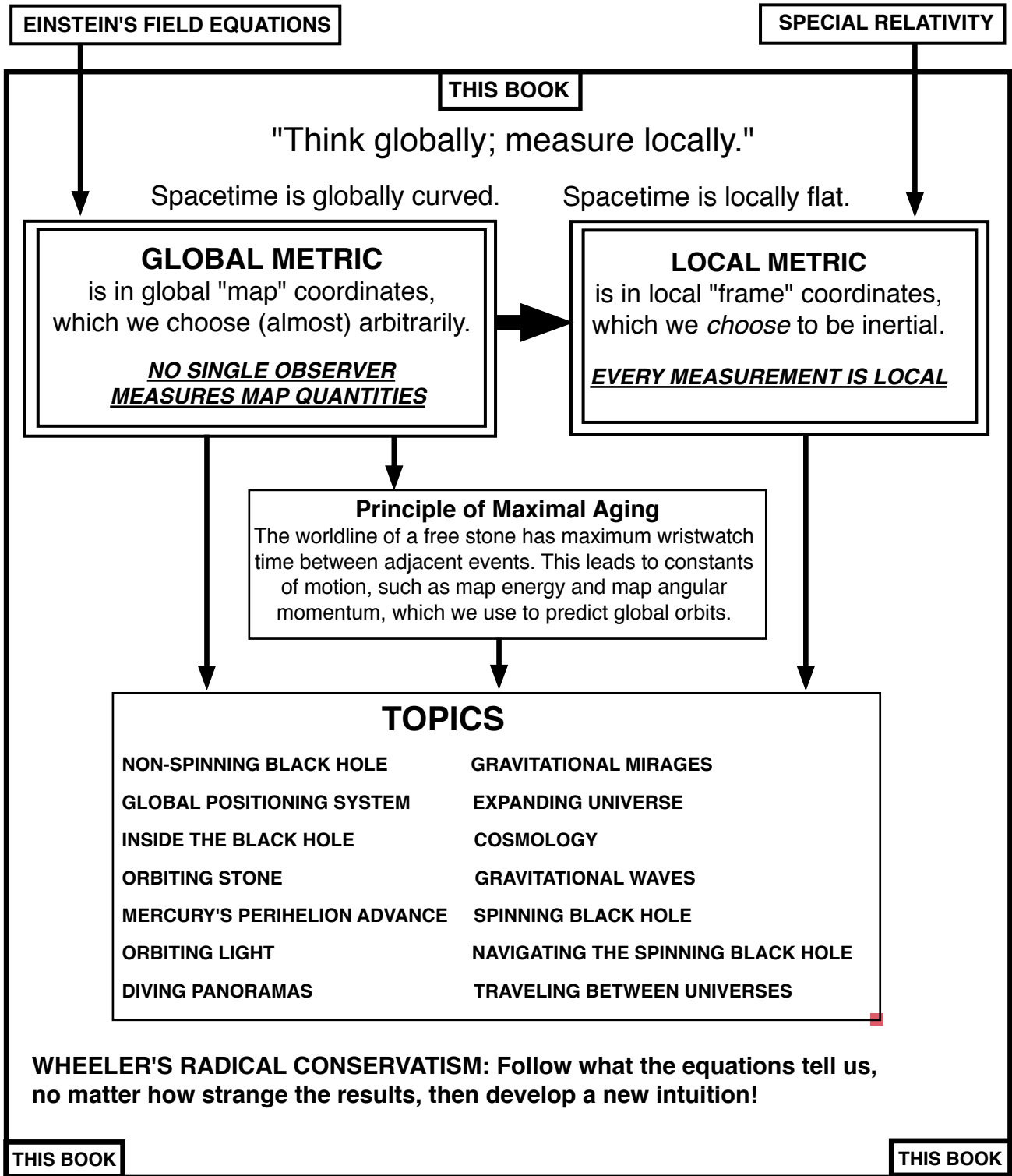
Our strategy has two parts: The metric and the Principle of Maximal Aging. First the metric:

- Choose to index each event in curved spacetime with an arbitrarily chosen set of global coordinates, which we call *map coordinates*. Submit these map coordinates to Einstein's field equations, which return the *global metric*. The input to the global metric is the differential separation in global map coordinates between two adjacent events. The output of the global metric is the differential of a measurable quantity.
- One of several measurable quantities is the *wristwatch time*, the time between two events measured on a wristwatch that moves directly from one event to its neighbor.
- Next, we "elbow" the differentially small region of spacetime of the metric into a slightly larger region in which to construct a local inertial frame big enough to carry out our desired measurement. In this region the exact differential global metric becomes an approximate local metric that separates space and time for analysis by special relativity.
- Finally, the global metric allows us to connect measurements of, say, a fast-moving particle that passes along a *worldline* across one local inertial frame, then across a second local inertial frame far from the first.

The second part of our strategy: The Principle of Maximal Aging, tells the stone how to move:

The worldline of a free stone has maximum wristwatch time between adjacent events. This leads to global constants of motion, such as map energy and map angular momentum, which we use to predict global orbits.

This double strategy is diagrammed on the back cover of the book, reproduced on the following page.



**KEY IDEAS:** Just three words summarize this book: spacetime, motion, measurement!  
 The global metric--with arbitrary global coordinates--describes spacetime.  
 The Principle of Maximal Aging describes free motion.  
 Choose to report every measurement with respect to a local inertial frame.

# To Assemble the Book

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YOU MAY download just one chapter or other element of the book for personal study or class use. However, IF you wish to assemble the entire book, THEN . . .

WE SUGGEST THAT YOU PRINT as bookends the Front Cover, Front Matter, Contents, Inside Back Cover, and Back cover, and then individual chapters as you need them, placed between Contents and Inside Back Cover.

## DOCUMENT FORMAT AND DATING CODE

Simply DOUBLE-CLICK on each file to download it. All files are in the "portable document format" with the file extension .pdf. Every file name ends with a code for the date of that version. This code has the form YYMMDDv# (Year, Month, Date, Version number on that date). For example, the first chapter might have the file name Ch01Speeding170622v3.pdf. Translation: The third version of the first chapter, called Speeding, created on June 22, 2017. PAY ATTENTION to this date code; we may revise or update any file at any time.

Print each CHAPTER on two sides of every sheet, with odd-numbered pages on the right. This means that the unnumbered initial page -- containing chapter contents and teaser questions -- will be a left-hand page facing the chapter's first page.

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## FILES ON THIS DOWNLOAD WEBSITE:

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AAAFrontCover

AAFrontMatter

Constants and conversion factors. Fifty-seven questions.

AContents

With a brief description of every chapter.

Chapter 1 Speeding

Special relativity presented so as to lead naturally to general relativity

Chapter 2 The Bridge: SR to GR

What is the difference between flat spacetime and curved spacetime?

Chapter 3 Curving

Describe curved spacetime outside Earth and down to the center of a non-spinning black hole.

Chapter 4 The Global Positioning System (GPS)

Locate yourself anywhere on Earth with a hand-held device which is useless without general relativity.

Chapter 5 Global and Local Metrics

Over a sufficiently small region of spacetime, special relativity correctly describes every measurement.

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100	Chapter 6 Diving
101	Dive into a black hole. How do you feel? How long do you live? Why do you die?
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103	Chapter 7 Inside the Black Hole
104	A relaxed life with spectacular effects around you and an ending certain.
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106	Chapter 8 Circular Orbits
107	What circular "parking" orbits are available to you near a black hole?
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109	Chapter 9 Orbiting
110	Transfer between circular "parking" orbits. Close to the black hole, killer tides threaten humans and
111	robots.
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113	Chapter 10 Advance of Mercury's Perihelion
114	An early victory of Einstein's brand new general relativity theory.
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116	Chapter 11 Orbits of Light
117	Trajectories of light around a black hole.
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119	Chapter 12 Diving Panoramas
120	What changing panoramas surround you as you drop into a black hole? What is the last thing you see?
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122	Chapter 13 Gravitational Mirages
123	Stars, galaxies, and black holes act like distorting lenses as we look outward into the Universe.
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125	Chapter 14 Expanding Universe
126	The shape in space and time of an expanding universe.
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128	Chapter 15 Cosmology
129	Ordinary matter? Dark matter? Dark energy? The Big Bang and its consequences.
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131	Chapter 16 Gravitational Waves
132	Gravitational waves tell us about cosmic catastrophes and regions close to the monster black hole.
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134	Chapter 17 Spinning Black Hole
135	Irresistible motion, multiple horizons, falling with a raindrop.
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137	Chapter 18 Circular Orbits around the Spinning Black Hole
138	Circular orbits far from and close to a spinning black hole. The accretion disk powers a quasar.
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140	Chapter 19 Orbiting the Spinning Black Hole
141	Moving between circular orbits near a spinning black hole
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143	Chapter 20 Orbits of Light around the Spinning Black Hole
144	What do you see as you orbit around and plunge into a spinning black hole
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146	Chapter 21 Travel Through the SpinningBH
147	Pass inward through the horizon of the spinning black hole; emerge into another Universe.
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149 Chapter 22 Deriving the Metric  
150 (To be written) Einstein's field equations for static spherical spacetimes; derive the Schwarzschild  
151 metric. Metrics for spherical stars, charged black holes, white holes, wormholes, and inflationary  
152 cosmology.

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154 V Appendix A Wheeler's Rules of Writing  
155 Motivate! Simplify! Self-descriptive terminology, and the dullness of simply being.

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157 W Appendix B Glossary  
158 Words forbidden in our book. Definitions of permitted words.

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160 X Appendix C Acknowledgments

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162 Y Inside the Back Cover  
163 General relativity briefing

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165 Z Back Cover  
166 Diagrammed strategy of this book

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168 *The spinless black hole is like a spinning black hole, but its gate to other universes is closed.*  
169 *For the spinning black hole, this gate is ajar.*

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171 --- Luc Longtin

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173 SOFTWARE GRorbits  
174 The interactive software program GRorbits, by Slavomir Tuleja, plots many figures in the book and is  
175 available for the reader to plot orbits of a stone or a light flash around a black hole, predicted by three  
176 alternative theories:

- 177  
178 1. Newtonian mechanics  
179 2. general relativity on a flat plane through the center of a non-spinning black hole  
180 3. general relativity on the flat symmetry plane -- the equator -- of a spinning black hole, with arbitrary  
181 mass and any value of spin permitted by the theory.

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183 Here is the link to the GRorbits website: <http://stuleja.org/grorbits/>  
184 Here is the direct link to the GRorbits download site: <http://stuleja.org/grorbits/run.html>

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186 For Mac users, this puts GRorbits into the Applications folder.

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188 Please note, there are some pre-programmed scenarios which can be downloaded for use by the  
189 GRorbits program, obtained from <http://stuleja.org/grorbits/scenarios.html>

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191 PS1. EXERCISES. Early chapters have lots of exercises. Later chapters have fewer. For exercise  
192 assignments, the instructor may ask you to solve one or more QUERIES in the body of the chapter.

193  
194 PS2. WHAT HAPPENED TO THE FIRST EDITION of *Exploring Black Holes* by Edwin F. Taylor  
195 and John Archibald Wheeler? The first edition is now out of print. The original publisher no longer  
196 exists. Copies of the first edition are available online at exorbitant prices. In contrast, the contents of  
197 this draft second edition, from this dropsite, contain more material, is more up to date, and is free.

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*"Man fears time, but time fears the pyramids"* by "The learned Arab of the twelfth century" (quot. 1923) who has not been identified.

#### CORRECTIONS? OBJECTIONS? SUGGESTIONS?

FOR EBH2e and this README file:

Nandor Bokor at [n\\_bokor@yahoo.com](mailto:n_bokor@yahoo.com)  
born 1969

Edwin Taylor at [eftaylor631@gmail.com](mailto:eftaylor631@gmail.com)  
born 1931

FOR the interactive software program GRorbits:

Slavo Tuleja at [stuleja@gmail.com](mailto:stuleja@gmail.com)

John Archibald Wheeler  
1911 - 2008

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LUC LONGTIN, a professional legal French-English translator, made black holes an avocation -- a hobby. His detailed comments and suggestion on endless drafts of EBH2e corrected the physics and clarified the logic of presentation.

JOHN ROGOSICH, President of Techsetters, Inc., contributed his services to design, redesign, and continually upgrade the LaTeX format of chapters under the demanding requirements of authors and reviewers. The LaTeX style file has the name EBH.sty

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